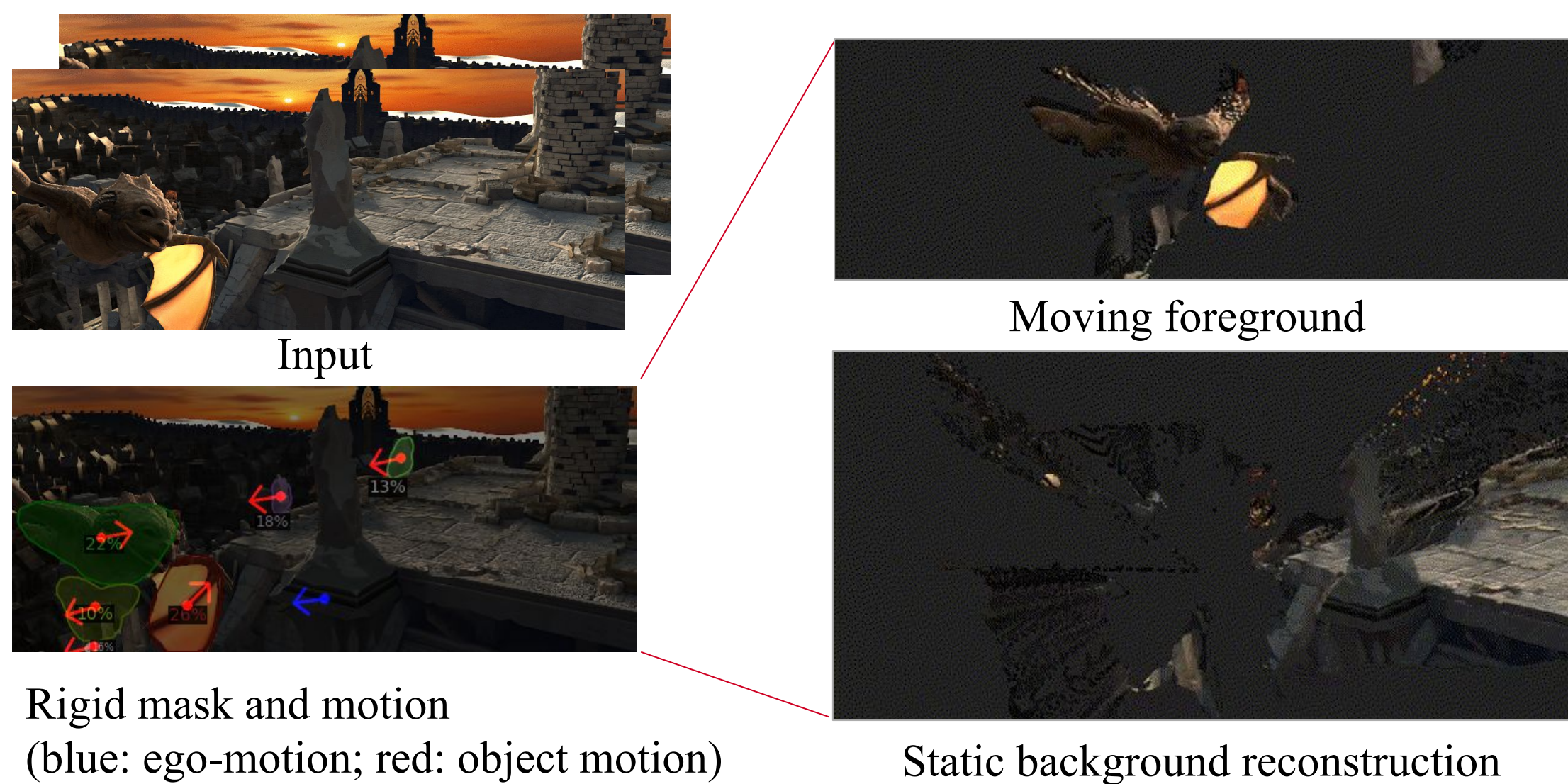


Goal: Scene decomposition based on two-frame rigidity



Related work

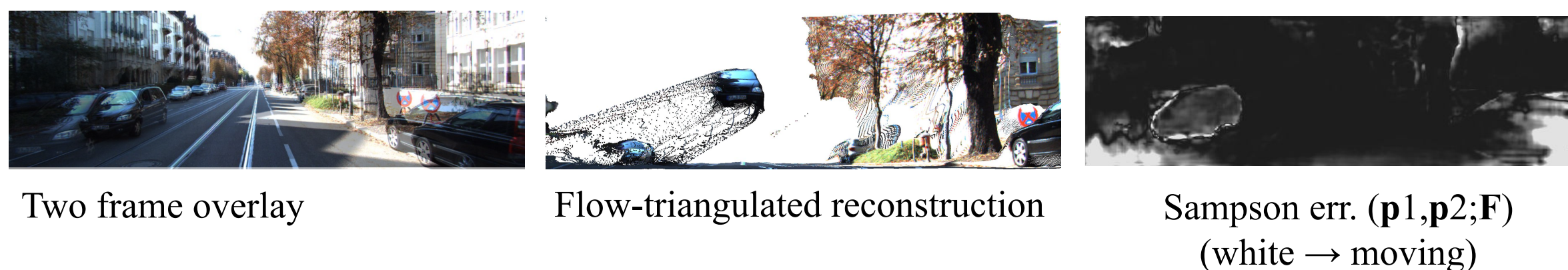


Geometric Motion segmentation (2D motion angle) [1,2] Appearance-based detectors (fires on objects *able to move*) Ours (fires only on *moving* objects)

[1] P Bideau and E Learned-Miller. "It's moving! A probabilistic model for causal motion segmentation in moving camera videos." ECCV. 2016.
 [2] J Wulff, L Sevilla-Lara, MJ Black. "Optical flow in mostly rigid scenes." CVPR. 2017.

Challenges

- Degeneracies in geometric motion segmentation.
 - Epipolar constraints fail when translation is close to zero.
 - Points moving along epipolar lines cannot be distinguished.
- Noisy motion correspondences and camera egomotion estimates.

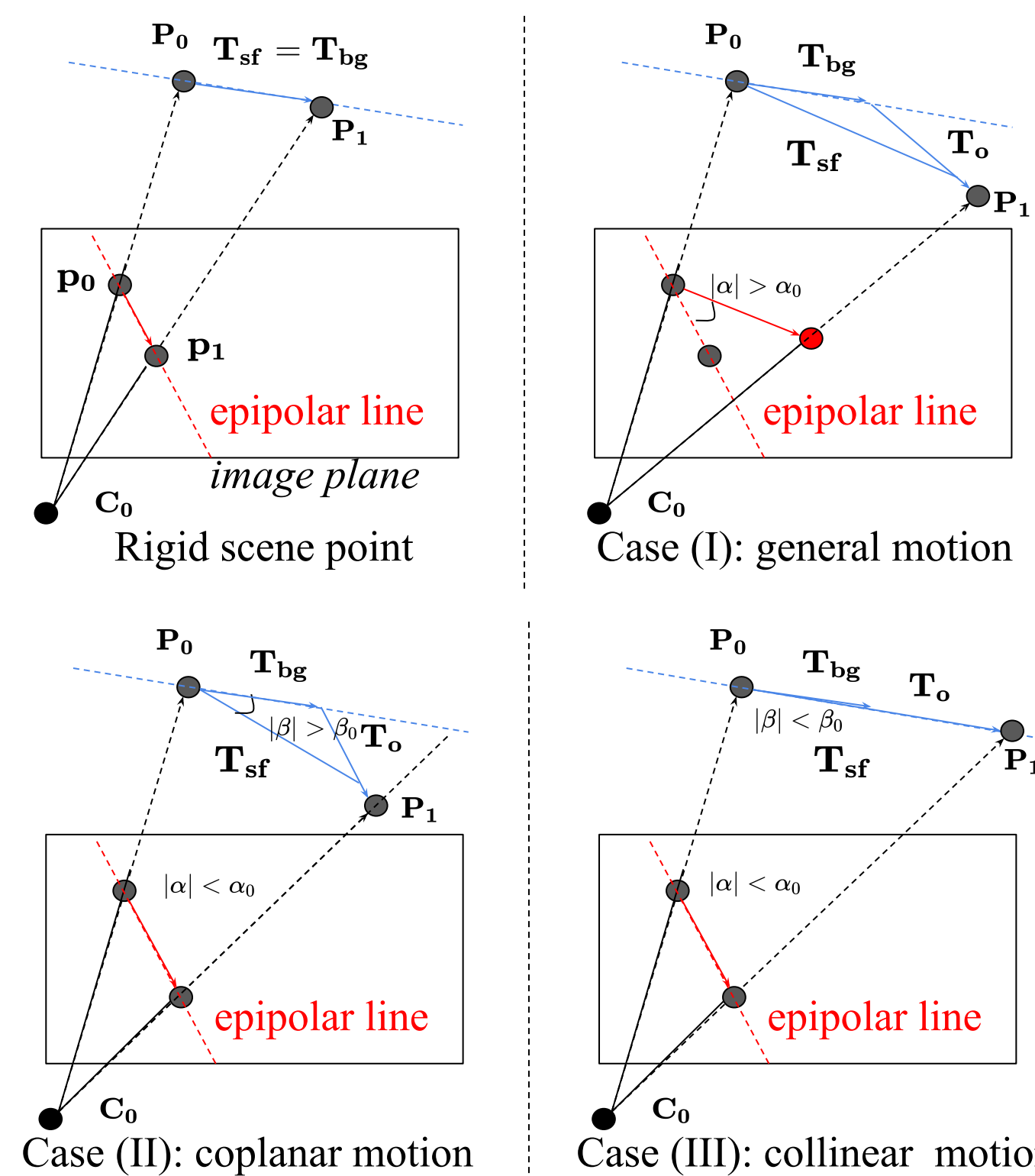


Analysis

When can a moving scene point P be identified from a moving camera?

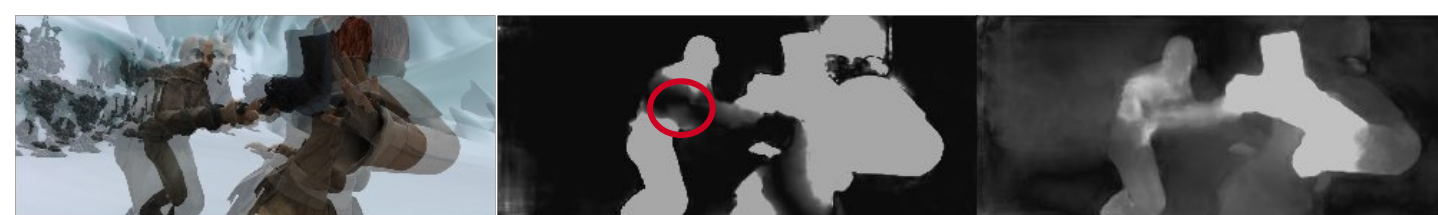
$$\mathbf{T}_{bg} := -\mathbf{T}_c \quad (\text{bg motion due to camera motion})$$

$$\mathbf{T}_{sf} := \mathbf{P}_1 - \mathbf{P}_0 \quad (\text{3D scene flow assuming no cam rotation})$$



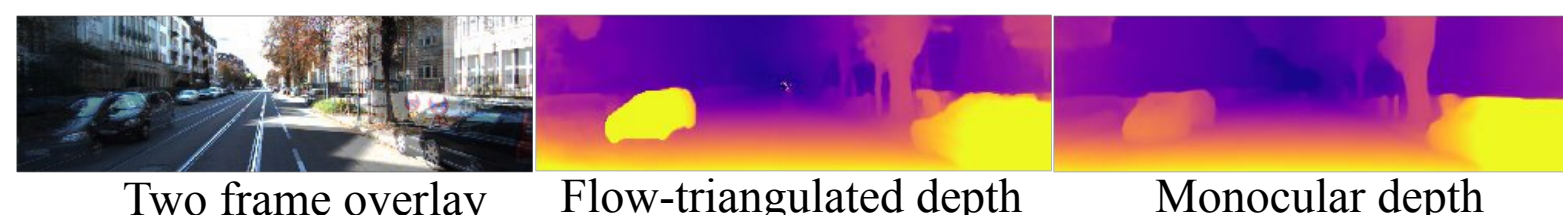
Degeneracies and rigidity cost maps

- **Small translation:** Rotational homography $c_H(\mathbf{p}_0, \mathbf{p}_1; \mathbf{H}_R)$
- **Coplanar motion** (ambiguous w/o relative depth $\tau=Z_1/Z_0$)



$$c_{3D\text{-angle}}(\mathbf{p}_0, \mathbf{p}_1, \tau; \hat{\mathbf{T}}_{bg}, \mathbf{H}_R) = |\angle(\hat{\mathbf{T}}_{bg}, \hat{\mathbf{T}}_{sf})|, \quad \hat{\mathbf{T}}_{sf} = \mathbf{K}_0^{-1}(\tau \mathbf{H}_R \mathbf{p}_1 - \mathbf{p}_0)$$

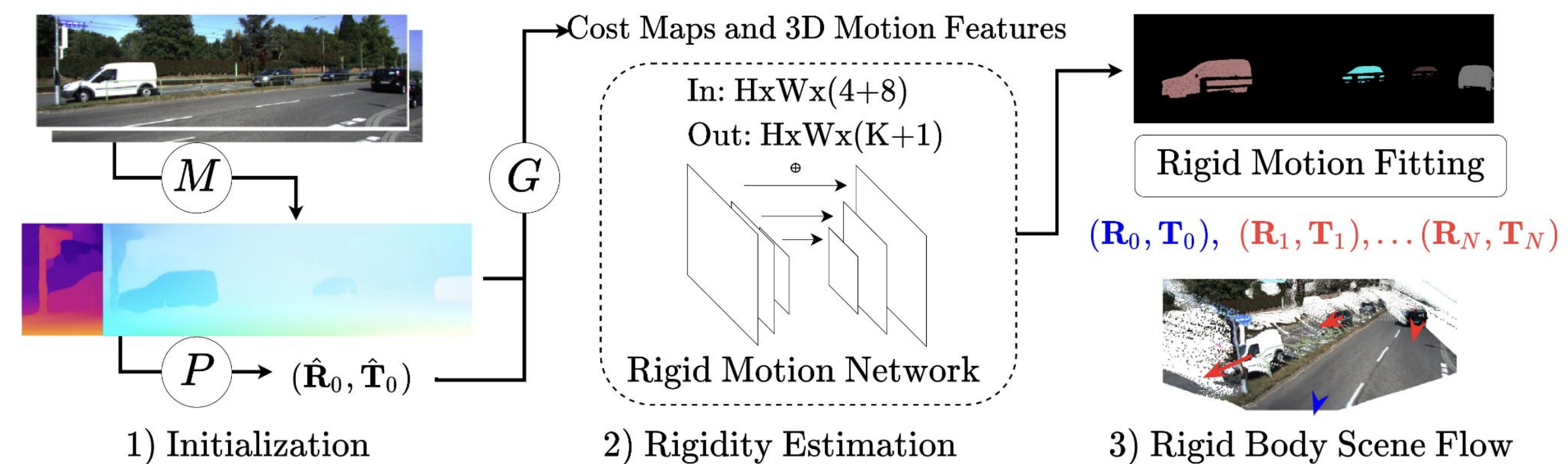
- **Collinear motion** (ambiguous w/o 1st frame depth Z_0)



$$c_{\text{depth}}(\mathbf{p}_0, \mathbf{p}_1, Z_0; \hat{\mathbf{T}}_{bg}, \mathbf{R}_{bg}) = \left| \log\left(\frac{Z_0}{Z_{flow}}\right) \right|, \quad Z_{flow} = \text{triangulate}(\mathbf{p}_0, \mathbf{p}_1; \hat{\mathbf{T}}_{bg}, \mathbf{R}_{bg})$$

"scale factor to align two depth maps for solving monocular scale ambiguity"

Pipeline



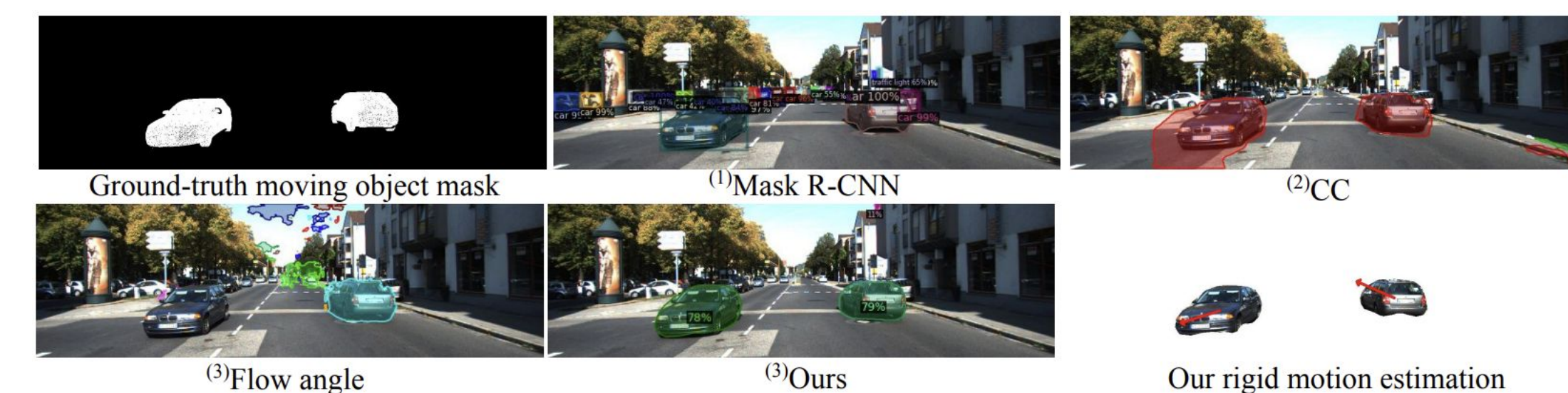
Losses

$$L = L_{\text{binary}} + L_{\text{center}} + L_{\text{polar}}$$



Results

Rigid motion segmentation



Stereo scene flow

	Method	K: obj \uparrow	K: bg \uparrow	S: bg \uparrow
(1)	Mask R-CNN [57]	88.20	96.42	81.98
	U ² (Saliency) [37]	64.80*	93.34	82.01
	MR-Flow-S (K) [58]	75.59*	94.70 [‡]	76.11
	MR-Flow-S (S) [58]	11.11*	84.72	92.64 [‡]
(2)	FSEG [24]	85.08*	96.27	80.22
	MAT-Net [67]	68.40*	93.08	77.95
	COSNet [30]	66.67*	93.03	80.86
	CC [39]	50.87*	85.50	\times
(3)	RTN [31]	34.29*	84.44	64.86
	FSEG-Motion [24]	61.29	89.41	78.25
	CC-Motion [39]	42.99	74.06	\times
	Flow angle [5, 58]	25.83	85.52	74.23
	Ours	90.71	97.05	86.72

	Method	D1* \downarrow	D2 \downarrow	F1 \downarrow	SF \downarrow
Ours Mask R-CNN	PRSM [54]	4.27	6.79	6.68	8.97
	OpticalExp [63]	1.81	4.25	6.30	8.12
	DRISF [32]	2.55	4.04	4.73	6.31
	Ours Mask R-CNN	1.89	3.42	4.26	5.61
	Ours Rigid Mask	1.89	3.23	3.50	4.89

Ablation study

Method	K: obj \uparrow	K: bg \uparrow	S: bg \uparrow
Reference	89.53	97.22	84.63
(1) w/o cost maps	88.66	96.59	76.81
(2) w/o uncertainty	85.09	95.72	77.25
(3) w/o monocular depth	84.46	94.84	76.14
(4) w/o expansion (MoA [6])	81.28	95.50	77.00
(5) w/o learning [5, 58]	25.83	85.52	74.23